Research Article

# **Dependence of Nuclear Flow on Different Parts of Nuclear Interaction Potential**

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#### **ABSTRACT:**

**Background:** During a heavy ion reaction, the interaction between projectile and target nucleons takes place and the outcome of a reaction depends strongly on the nuclear interaction potential, which is the imperative factor in deciding the fate of reaction. Several efforts have been made in this direction to explore number of phenomena. One of the most sought after phenomena in this direction is the collective flow and its various forms.

**Purpose:** This study aims to investigate the dependence of collective nuclear flow on different parts of nucleon-nucleon interaction potential for different mass asymmetric reactions  $^{129}Xe + ^{124}Sn$  ( $\eta = 0$ ),  $^{82}Kr + ^{158}Gd$  ( $\eta = 0.3$ ),  $^{56}Fe +$ <sup>184</sup>W ( $\eta$  = 0.5) and <sup>35</sup>Cl + <sup>205</sup>Tl ( $\eta$  = 0.7) by keeping A<sub>total</sub> = 240 units. Two different signatures of collective flow have been studied: a) bounce-off of compressed matter in the reaction plane called directed flow and b) squeeze-out of the participant matter out of the reaction plane called elliptical flow.

**Methods:** The present work is carried out within the Isospin dependent Quantum Molecular Theoretical Framework in which total interaction potential is composed of Skyrme potential, Yukawa Potential, Coulomb Potential, Momentum dependent interaction potential and symmetry potential.

**Results:** The findings reveal that the directed flow increases with addition of momentum dependent interactions and symmetry potential while the elliptical flow tend to decrease with addition of these potentials.

**Conclusions:** Both the momentum dependent interaction potential and symmetry potential have sizable affect on the magnitude of collective nuclear flow. A comparison between our calculations and experimental data for the energy dependence of elliptical flow for  $_{50}^{129}$ Xe +  $_{50}^{124}$ Sn reaction reveals that all the components of nuclear potential are necessary to explain the reaction dynamics.

**Keywords:** Nuclear interaction potential, Nuclear flow, Mass asymmetry, Momentum dependent potential, Symmetry potential.

#### **1. Introduction**

The heavy ion (HI) collisions are the eloquent tool to probe the nuclear matter under the extreme conditions of temperature and density in terrestrial laboratory. Several efforts, during past decades, have been made to study the thermodynamic properties of this matter and to shed light on dynamics of its formation and subsequent disintegration [\[1\]](#page-5-0). Among different observables, the collective motion of particles in HI collisions has been a topic of interest since it gives physical insight into the dynamical evolution of compressed and hot nuclear matter. It is depicted by the space-momentum correlations which are of dynamic origin, which are

explored via study of directed and elliptical flow.The directed flow also called in-plane flow and the elliptic flow also called out-of-plane flow are two different components widely studied in HIC at intermediate energies [\[2,](#page-5-1) [3\]](#page-5-2).

If the beam direction is along z-axis and impact parameter is along x-axis, then x-z plane is defined as reaction plane and x-y plane as azimuthal plane, characterizing the azimuthal distribution of particles. Consider  $\phi$  is the azimuthal angle between the reaction plane and transverse momenta of emitted particles, then the flow can be represented mathematically as

Fourier expansion  $[4, 5]$  $[4, 5]$  $[4, 5]$ , given as:

$$
\frac{dN}{d\phi} = 1 + 2\sum_{n=1}^{\infty} v_n \cos(n\phi)
$$
 (1)

where  $v_n$ , the flow parameter, is called nth harmonic function or Fourier coefficient of Fourier expansion where,  $n = 1, 2, 3, \ldots$  and so on. The first two harmonics,  $v_1$  and  $v_2$  are the directed flow and elliptical flow, respectively. The directed and elliptical flow are defined as:

$$
v_1 = \langle \cos \phi \rangle = \langle \frac{p_x}{p_t} \rangle; \tag{2}
$$

$$
v_2 = <\cos 2\phi> = <\frac{p_x^2 - p_y^2}{p_t}
$$
 (3)

where  $p_x$  is the transverse momentum gained by the emitted particle and  $p_t$  is the mean transverse momentum given by,  $p_t = \sqrt{p_x^2 + p_y^2}$ , where  $p_x$  and  $p_y$  being the x and y components of momentum. The elliptical flow gives the elliptical distribution of outgoing particles in the reaction plane  $[6, 7]$  $[6, 7]$  $[6, 7]$ . The positive value of  $v_2$  portrays the in-plane emission of particles while the negative values of  $v_2$  describes the squeeze-out in direction perpendicular to the reaction plane. Several experimental collaborations such as FOPI, INDRA are involved in the study of elliptical flow ranging from Fermi to ultra-relativistic energies [\[8,](#page-5-7) [9\]](#page-5-8). At low energies, the directed flow observables are closely connected to interplay between mean field and nucleonnucleon collisions and evolves with energy [\[10\]](#page-6-0). The elliptical flow arises from expansion of compressed participant zone, which is possibly affected by shadowning effect of spectator matter [\[11\]](#page-6-1).

The dependence of collective flow on different factors such as colliding geometry, radii of nuclei, projectile energy, mass of colliding nuclei, isospin has divulged stimulating physics involving origin of collective flow and its properties [\[12,](#page-6-2) [13,](#page-6-3) [14\]](#page-6-4). The study of excitation function of collective flow shows it is negative at low energies as the interaction is governed by attractive component of mean field. But at higher energies, in addition to mean field the repulsive nucleon-nucleon (NN) interactions become significant, resulting in deflection of emitted particles in direction

of incident projectile i.e. positive angles. This continuous evolution of flow with increase in energy from negative to positive becomes zero at a particular value of energy, coined as balance energy( $E_{bal}$ ), where the attractive mean field is counter balanced by repulsive NN interactions. These studies revealed the strength of transverse flow and  $E_{bal}$  which facilitate to probe the nuclear equation equation of state (NEOS) and in-medium NN cross-sections [\[15,](#page-6-5) [16,](#page-6-6) [17\]](#page-6-7).

Many researchers have made efforts in the literature to investigate the mechanism behind heavy ion collisions and multi fragmentation employing the NN interaction potential [\[18,](#page-6-8) [19,](#page-6-9) [20\]](#page-6-10), but the contribution of different parts of NN interaction potential towards collective flow needs further investigation. Therefore we intend to investigate the dependence of collective flow and reaction dynamics on different parts of NN interaction potential in mass asymmetric collisions.

In section 2, brief methodology of the dynamical approach used to interpret experimental results is presented. Results are discussed in section 3. Finally, the conclusions are presented in section 4.

### **2. Method and Materials: Theoretical Framework**

The present work is carried out within the Isospin dependent Quantum Molecular Theoretical Framework [\[21,](#page-6-11) [22\]](#page-6-12), a modernized version of the QMD model developed by Aichelin and co-workers [\[23,](#page-6-13) [24,](#page-6-14) [25,](#page-6-15) [26\]](#page-6-16). The IQMD model has been used successfully to explain various phenomena such as fragmentation [\[27,](#page-6-17) [28\]](#page-6-18), collective flow [\[29,](#page-6-19) [30\]](#page-7-0), elliptical flow [\[31\]](#page-7-1) successfully. The isospin degree of freedom enters into the calculations via symmetry potential, cross-sections and Coulomb interactions. In IQMD model, the nucleons of target and projectile interact via two and three-body Skyrme forces, Yukawa potential and Coulomb interactions. In addition to the use of explicit charge states of all baryons and mesons, a symmetry potential between protons and neutrons corresponding to the Bethe-Weizsacker mass formula has been included. In

this model, baryons are represented by wave packet

$$
f_i(\vec{r}, \vec{p}, t) = \frac{1}{(\pi \hbar)^3} \cdot e^{-(\vec{r} - \vec{r}_i(t))^2 / 2L} \cdot e^{-(\vec{p} - \vec{p}_i(t))^2 2L/\hbar^2}.
$$
\n(4)

The centroids of these wave packets propagate using classical Hamilton equations of motion:

$$
\frac{d\vec{r}_i}{dt} = \frac{d\langle H \rangle}{d\vec{p}_i} \; ; \; \frac{d\vec{p}_i}{dt} = -\frac{d\langle H \rangle}{d\vec{r}_i} \tag{5}
$$

with

$$
\langle H \rangle = \langle T \rangle + \langle V \rangle
$$
  
= 
$$
\sum_{i} \frac{p_i^2}{2m_i} + \sum_{i} \sum_{j>i} \int f_i(\vec{r}, \vec{p}, t) V^{ij}(\vec{r}', \vec{r})
$$
  

$$
\times f_j(\vec{r}', \vec{p}', t) d\vec{r} d\vec{r}' d\vec{p} d\vec{p}'
$$
 (6)

The baryon-baryon potential  $V^{ij}$ , in the above relation, reads as:

$$
V^{ij}(\vec{r}' - \vec{r}) = V^{ij}_{Skyrme} + V^{ij}_{Yukawa} + V^{ij}_{Coul} + (7)
$$
  
\n
$$
V^{ij}_{sym} + V^{ij}_{MDI}
$$
  
\n
$$
= t_1 \delta(\vec{r}' - \vec{r}) + t_2 \delta(\vec{r}' - \vec{r}) \rho^{\gamma - 1} \left(\frac{\vec{r}' + \vec{r}}{2}\right)
$$
  
\n
$$
+ t_3 \frac{exp(-|\vec{r}' - \vec{r}|/\mu)}{(|\vec{r}' - \vec{r}|/\mu)} + \frac{Z_i Z_j e^2}{|\vec{r}' - \vec{r}|}
$$
  
\n
$$
+ t_4 \frac{1}{\rho_0} T_3^i T_3^j \delta(\vec{r}' - \vec{r})
$$
  
\n
$$
+ t_5 ln^2 [t_6(\vec{p}' - \vec{p})^2 + 1] \delta(\vec{r}' - \vec{r})
$$
(8)

Here  $Z_i$  and  $Z_j$  denote the charges of  $i^{th}$  and  $j<sup>th</sup>$  baryon. The parameters  $\mu$  and  $t_1, \ldots, t_6$  are adjusted to the real part of the nucleonic optical potential. This interaction potential basically consists of different parts, viz."density-dependent Skyrme potential, repulsive Coloumb potential, Yukawa surface potential, momentum-dependent interaction potential and symmetry potential". The Skyrme is the basic potential that corresponds to the nuclear matter density. The inclusion of Yukawa term improves the surface properties of nuclei, and is considered important for fragment formation. The Coulomb potential comes into picture in case of charged particles and thus, contribute towards the repulsive interaction between protons. Since these interactions are absent for neutrons, so this potential, sometimes, has also been treated as a part of isospin effects which differentiate the protons from neutrons. Likewise, the role of momentum-dependent potential (usually at high incident energies) during initial phase of a collision is established as well, when relative momentum between projectile and target nucleons is high [\[32\]](#page-7-2). Lastly, nuclear symmetry potential plays a significant role in nuclear collisions involving isospin (neutron-proton) asymmetric colliding partners. Thus, every term in NN interaction potential is important and plays significant role depending upon entrance channel parameters. However, there is a significant impact of these potential's on fragment production and collective flow at intermediate energies. The term "flow" is usually understood as a phenomenological description of a collective expansion, and the theoretical models are quite successful in describing the observed features of the experimental data available in the literature.

### **3. Results and Discussions**

In the present work, several thousand events have been simulated for the semi-central collisions of the reactions  $^{129}Xe + ^{124}Sn$  ( $\eta = 0$ ),  $^{82}Kr + ^{158}Gd$  ( $\eta = 0.3$ ),  $^{56}Fe +$ <sup>184</sup>W ( $\eta = 0.5$ ) and <sup>35</sup>Cl + <sup>205</sup>Tl ( $\eta = 0.7$ ) at incident energies between 50 to 200 MeV/nucleon. In order to study the role of mass asymmetry of the reaction on collective flow, the reactions are chosen in such a way that the mass asymmetry of the reactions varies between 0 to 0.7 while the total mass remains constant i.e.  $A_{total} = 240$  units. A soft equation of state has been employed in present work and the observations are recorded at saturation time (i.e. 200 fm/c) because after this time, there is no further change in the phase space configuration of colliding nuclear matter.

To study the contribution of each component of nuclear interaction potential in different observables, one starts with the basic potential and then resimulate the reaction each time by adding gradually the other components of nuclear potential. Acronym SY stands for Skyrme + Yukawa potential, SYC stands for Skyrme + Yukawa + Coulomb potential, SYCM stands for Skyrme + Yukawa + Coulomb + momentum dependent potential, SYCMS stands for Skyrme + Yukawa + Coulomb + momentum dependence + symmetry potential and SYCMSd stands for Skyrme



**Figure 1:** Azimuthal angle dependence of  $dN/d(Cos2\phi)$  for  $Z = 2$  at  $E = 50$  MeV/nucleon for different set of potentials for  $129$ Xe+ $124$ Sn reaction. The minima occurring at  $2\phi = \pi/2$ depicts the prominence of in-plane emission whereas the peaks at  $2\phi = 0$  and  $\pi$  correspond to the preferred azimuthal emission in-plane and out-of-plane respectively.

+ Yukawa + Coulomb + momentum dependence + density dependent symmetry potential with  $\gamma = 0.66$ .

We begin with the azimuthal dependence of  $dN/d(Cos2\phi)$  for  $Z = 2$  particles at  $E = 50$  MeV/nucleon for  $129Xe+124Sn$  reaction for different set of potentials as shown in Fig. 1. It is clear that minima occurs at  $2\phi$  $= \pi/2$  depicting the prominence of azimuthal emission in-plane whereas the peaks at  $2\phi = 0$  and  $\pi$  corresponds to the preferred azimuthal emission in-plane and outof-plane. Moreover, the peak at  $2\phi = 0$  is higher in comparison to at  $2\phi = \pi$ , which indicates that number of particles emitted in-plane are large as compare to the number of particles emitted out-of-plane. This means that ellipse formed is not symmetric around the z-axis i.e in the collision of asymmetric nuclei the distribution of nucleon after the collision in momentum space is not uniform. Also, we note that with addition of MDI and symmetry potential, these peaks become

more pronounced due to an increase in pressure gradient in overlapping zone resulting due to additional repulsion generated by these potentials. Fig.2 shows



**Figure 2:** Energy dependence of reduced flow  $\partial v_1 / \partial Y^{red}$ at  $\hat{b} = 0.5$  fm for different set of potentials for <sup>129</sup>Xe+<sup>124</sup>Sn reaction.

the energy dependence of reduced flow in mid-rapidity region, where the nuclear matter compressibility is greater than the spectator region, for  $^{129}Xe + ^{124}Sn$  reaction. At low energies, due to Pauli blocking the NN collisions are blocked and mean field dominate the reaction dynamics leading to negative slope of reduced flow at low energies. But with an increase in energy, the dominance of NN collisions increases and hence slope rises. We note that with involvement of MDI and symmetry potential, the reduced flow rises more sharply since these potentials provide extra repulsion to the system.

Further, to illustrate the role of different parts of NN potential in elliptical flow, energy dependence of elliptical flow per nucleon for different asymmetric reactions <sup>129</sup>*Xe* + <sup>124</sup>*Sn* ( $\eta$  = 0), <sup>82</sup>*Kr* + <sup>158</sup>*Gd* ( $\eta$  = 0.3),  ${}^{56}Fe + {}^{184}W (\eta = 0.5)$  and  ${}^{35}Cl + {}^{205}Tl (\eta = 0.7)$ is shown for different set of potentials. Fig. 3 shows



**Figure 3:** Energy dependence of  $v_2$ /nucleon for <sup>82</sup>Kr+<sup>158</sup>Gd ( $\eta = 0.3$ ), <sup>56</sup>Kr+<sup>184</sup>W ( $\eta = 0.5$ ) and <sup>35</sup>Cl+<sup>205</sup>Tl ( $\eta = 0.7$ ) reactions.



**Figure 4:** Energy dependence of elliptic flow  $v_2$ /nucleons for Z = 2 at  $\hat{b} = 0.5$  fm for different set of potentials for  $129$ Xe+ $124$ Sn reaction along with comparison with experimental data.

that the elliptical flow per nucleon  $(v_2/nucleon)$  changes from positive to negative values with an increase in energy. As we move from nearly symmetric reaction  $(\eta = 0.3)$  to highly asymmetric reaction  $(\eta = 0.7)$ , the trend remains the same while the flow changes to more positive value. It can be associated with change in

dominance from mean field at low energies to binary nucleon-nucleon collisions at higher energies. Further, we extend this study to the energy dependence of elliptic flow for symmetric reaction <sup>129</sup> $Xe+$ <sup>124</sup> $Sn$  ( $\eta = 0$ ) in reference to available experimental data[\[34\]](#page-7-3) as shown in Fig. 4. Elliptical flow per nucleon shows a transition

from positive to negative values with an increase in energy. The rapidity cut of  $Y^{red} = |Y_{c.m.}/Y_{beam}| \le 0.1$ is in accordance with experimental data. We note that by taking into account both the MDI and symmetry potential, the comparison with experimental data [\[34\]](#page-7-3) is better. However, at  $E = 250$  MeV/nucleon the role of different parts of potential nearly diminishes due to increase in violence of reaction at higher energies.

### **4. Findings and Conclusion**

The role of different components of nucleon-nucleon interaction potential on collective nuclear flow has been explored by varying the mass asymmetry and keeping  $A_{total}$  =240 units fixed, within the theoretical framework. Although the different components of NN potential have remarkable role in fragment production yet the momentum dependent interactions and symmetry potential have sizable affect on the magnitude of collective nuclear flow. The comparison of energy dependence of elliptical flow for  $^{129}_{50}$ Xe +  $^{124}_{50}$ Sn reaction with experimental data reveals that all the components of nuclear potential are necessary to explain the reaction dynamics. In future, one can elaborate the influence of density dependent symmetry energy and isospin dependence of NN cross section on the above mentioned observables for highly asymmetric collisions. This can provide a challenge to the experimentalists to prove the theoretical findings. Additionally, colliding lighter projectiles with heavier targets can result in the creation of radioisotopes, which have valuable applications in medical science.

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